

RAMAKRISHNA MISSION VIVEKANANDA CENTENARY COLLEGE, RAHARA, KOLKATA
Undergraduate Admission Test: Mathematics Honours

Full Marks : 75

Time : 1 hour

Each question has only one correct answer

Each question carries 3 marks for correct answer and (–1) mark for wrong answer.

(The symbols have their usual meanings)

1. The period of $\sin^2 \theta$ is
 - a. π^2
 - b. π
 - c. π^3
 - d. $\frac{\pi}{2}$
2. The solution of $\sin x + \cos x = 1$ is
 - a. $x = 2n\pi$
 - b. $x = 2n\pi + \frac{\pi}{2}$
 - c. $x = n\pi + (-1)^n \frac{\pi}{4} - \frac{\pi}{4}$
 - d. None of these.
3. If the lengths of the sides of triangle are 3, 5, 7, then the largest angle of the triangle is
 - a. $\frac{\pi}{2}$
 - b. $\frac{5\pi}{6}$
 - c. $\frac{2\pi}{3}$
 - d. $\frac{3\pi}{4}$
4. The remainder left out when $8^{2n} - (62)^{2n+1}$ is divided by 9 is
 - a. 2
 - b. 7
 - c. 8
 - d. 9
5. The solution of the following linear programming problem:
Minimise, $z = 200x + 500y$
subject to the constraints:
 $x + 2y \geq 10, 3x + 4y \leq 24, x \geq 0, y \geq 0$ is
 - a. $z = 2300$, at (4, 3)
 - b. $z = 2100$, at (4, 3)
 - c. $z = 2300$, at (3, 4)
 - d. $z = 2100$, at (3, 4)
6. The number of complex numbers z such that
 $|z - 1| = |z + 1| = |z - i|$ equals
 - a. 0
 - b. 1
 - c. 2
 - d. None of these.

7. From a group of 9 peoples, 4 have to be selected. In how many ways can the 4 peoples be selected so that one of them is always in the team?
- 45
 - 49
 - 54
 - 56
8. The third term of geometric progression is 4, the product of the first 5 term is
- 4^3
 - 4^4
 - 4^5
 - None of these
9. The straight lines $x + y = 0$, $3x + y - 4 = 0$, $x + 3y - 4 = 0$ form a triangle which is
- isosceles
 - equilateral
 - right angled
 - none of these
10. The two circles $x^2 + y^2 = ax$ and $x^2 + y^2 = 1$ touch each other if
- $a = 2$
 - $|a| = 2$
 - $2|a| = 1$
 - $|a| = 1$
11. If $f: \mathbb{R} \rightarrow \mathbb{R}$ is a differentiable function such that $f(x + y) = f(x)f(y)$ for all x, y and $f(5) = 2$, $f'(0) = 3$, then $f'(5)$ is
- 0
 - 1
 - 6
 - 2
12. Consider the relations R_1 and R_2 defined as $a R_1 b \Leftrightarrow a^2 + b^2 = 1$ for all $a, b \in \mathbb{R}$ and $(a, b) R_2 (c, d) \Leftrightarrow a + d = b + c$ for all $(a, b), (c, d) \in \mathbb{N} \times \mathbb{N}$. Then
- R_1 and R_2 both are equivalence relations
 - only R_1 is an equivalence relation
 - only R_2 is an equivalence relation
 - neither R_1 nor R_2 is an equivalence relation
13. In a frequency distribution, the mean and median are 21 and 22 respectively, then its mode is approximately
- 20.5
 - 22.0
 - 24.0
 - 25.5
14. Let $E = \{1, 2, 3, 4\}$ and $F = \{1, 2\}$, then the number of onto functions from E to F is
- 14
 - 16
 - 12
 - 08

15. If $3^x = 4^{x-1}$, then $x =$
- $\frac{2 \log_3 2}{2 \log_3 2 - 1}$
 - $\frac{1}{2 - \log_2 3}$
 - $\frac{2}{1 - \log_4 3}$
 - $\frac{2 \log_2 3}{2 \log_2 3 - 1}$
16. Find the value of $\sin(2 \tan^{-1}(0.75))$
- 0.75
 - 1.5
 - 0.96
 - 0.5
17. If A is a square matrix such that $A^2 = A$, then $(I - A)^3 + A$ is equal to
- I
 - O
 - $I - A$
 - $I + A$
18. Which of the following function differentiable at $x = 0$?
- $\cos(|x|) + |x|$
 - $\cos(|x|) - |x|$
 - $\sin(|x|) + |x|$
 - $\sin(|x|) - |x|$
19. The absolute maximum value of $y = x^3 - 3x + 2$ in $0 \leq x \leq 2$ is
- 0
 - 2
 - 4
 - 6
20. Let $f: (-1, 1) \rightarrow \mathbb{R}$ be a continuous function. If $\int_0^{\sin x} f(t) dt = \frac{\sqrt{3}}{2} x$, then $f\left(\frac{\sqrt{3}}{2}\right) =$
- $\frac{\sqrt{3}}{2}$
 - $\sqrt{3}$
 - $\sqrt{\frac{3}{2}}$
 - $\frac{1}{2}$
21. The area bounded by the curves $y = |x^2 - 1|$ and $y = 1$ is
- $\frac{2}{3}(\sqrt{2} + 1)$
 - $\frac{4}{3}(\sqrt{2} - 1)$
 - $2(\sqrt{2} - 1)$
 - $\frac{8}{3}(\sqrt{2} - 1)$

22. If $\frac{dy}{dx} = \frac{xy}{x^2+y^2}$ with $y(1) = 1$, then a value of x satisfying $y(x) = e$ is

- a. $\sqrt{3}e$
- b. $\frac{\sqrt{3}}{2}e$
- c. $\sqrt{2}e$
- d. $\frac{e}{\sqrt{2}}$

23. If \vec{a} , \vec{b} and \vec{c} are unit vectors, then

$$|\vec{a} - \vec{b}|^2 + |\vec{b} - \vec{c}|^2 + |\vec{c} - \vec{a}|^2 \quad \text{does not exceed}$$

- a. 4
- b. 9
- c. 8
- d. 6

24. The shortest distance between the lines $\frac{x+7}{-6} = \frac{y-6}{7} = z$ and

$$\frac{7-x}{2} = y - 2 = z - 6 \text{ is}$$

- a. $2\sqrt{29}$
- b. 1
- c. $\sqrt{\frac{37}{29}}$
- d. $\frac{\sqrt{29}}{2}$

25. Two numbers are selected randomly from the integers $\{1, 2, \dots, 9\}$. If the sum of the chosen two integers is even, then the probability that both the numbers are odd will be

- a. $\frac{2}{9}$
- b. $\frac{5}{8}$
- c. $\frac{3}{8}$
- d. $\frac{1}{9}$